

Cosmology With a Very Light $L_\mu - L_\tau$ Gauge Boson

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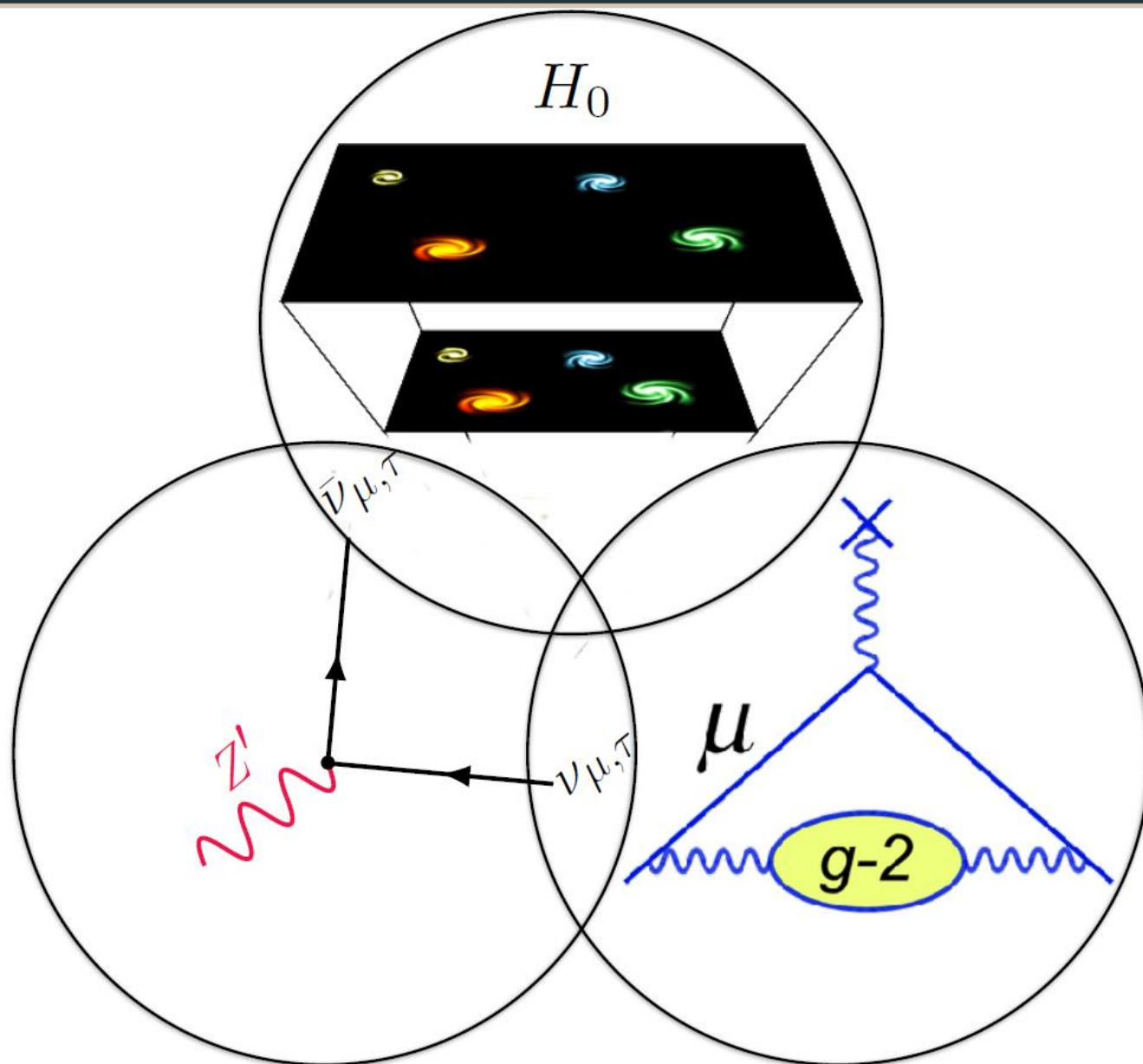
Dark Side of the Universe

July 16th, 2019 Buenos Aires

The 15th International Conference on the
DARK SIDE OF THE UNIVERSE

Based on [1901.02010] with M. Escudero, D. Hooper & G. Krnjaic

Outline



Contents

I. Motivation : H_0 and $(g - 2)_\mu$

1. The $(g - 2)_\mu$ discrepancy
2. The H_0 tension

II. A very light L_μ - L_τ gauge boson

1. The model
2. Different regimes

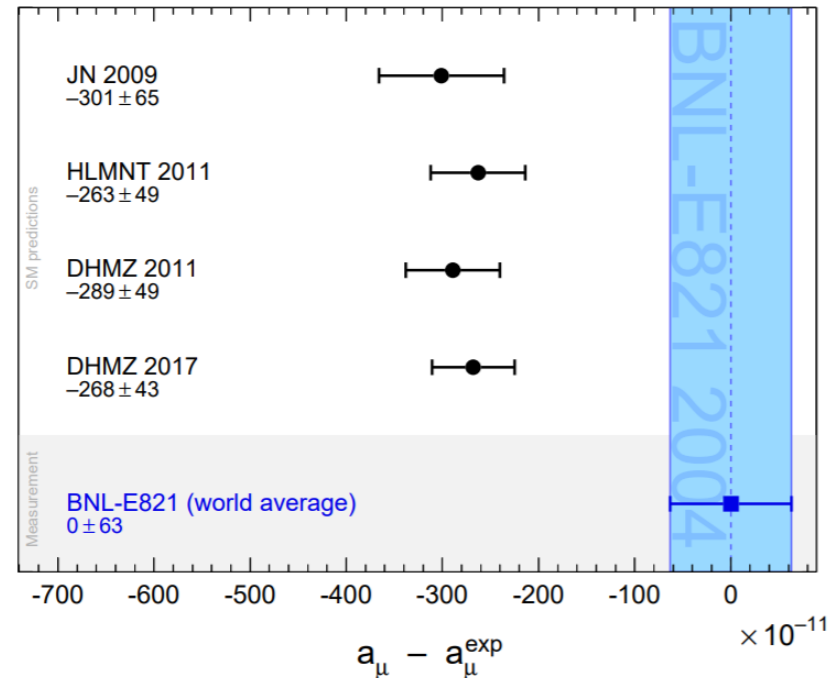
III. Results and conclusion

The $(g - 2)_\mu$ anomaly

$$\vec{\mu}_\mu = g_\mu \frac{\sqrt{4\pi\alpha}}{2m_\mu} \vec{S}_\mu \quad a_\mu \equiv \frac{g_\mu - 2}{2}$$

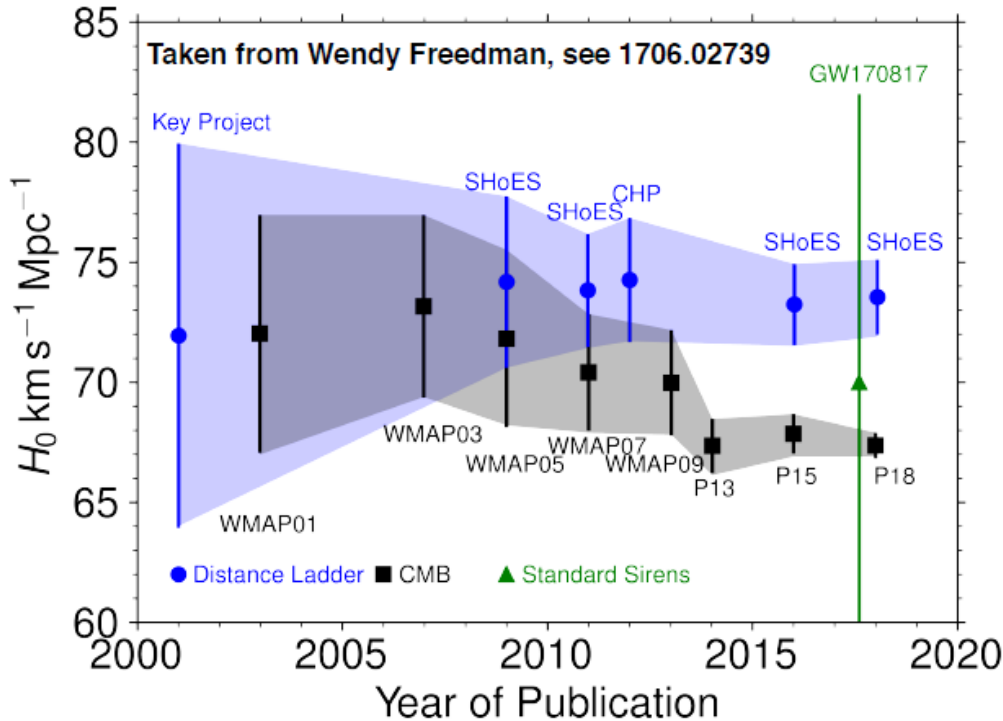
- Long standing $\sim 3.5\sigma$ discrepancy
 $\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 268(63)(43) \times 10^{-11}$
[PDG]

- SM prediction very **robust**
[Blum et al. 1311.2198]



- Many BSM interpretations SUSY, extra Higgses and symmetries
[Lindner et al. 1610.06587]
- **Fermilab** should reduce error by a factor ~ 4 : early 2019?
- Experiment at **J-PARC** should reach same sensitivity

The Hubble tension



Riess *et al* 1801.01120, 1804.10655

$$H_0 = 73.45 \pm 1.66 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

3.5 σ tension!

$$H_0 = 67.27 \pm 0.60 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Planck 2018 1807.06209

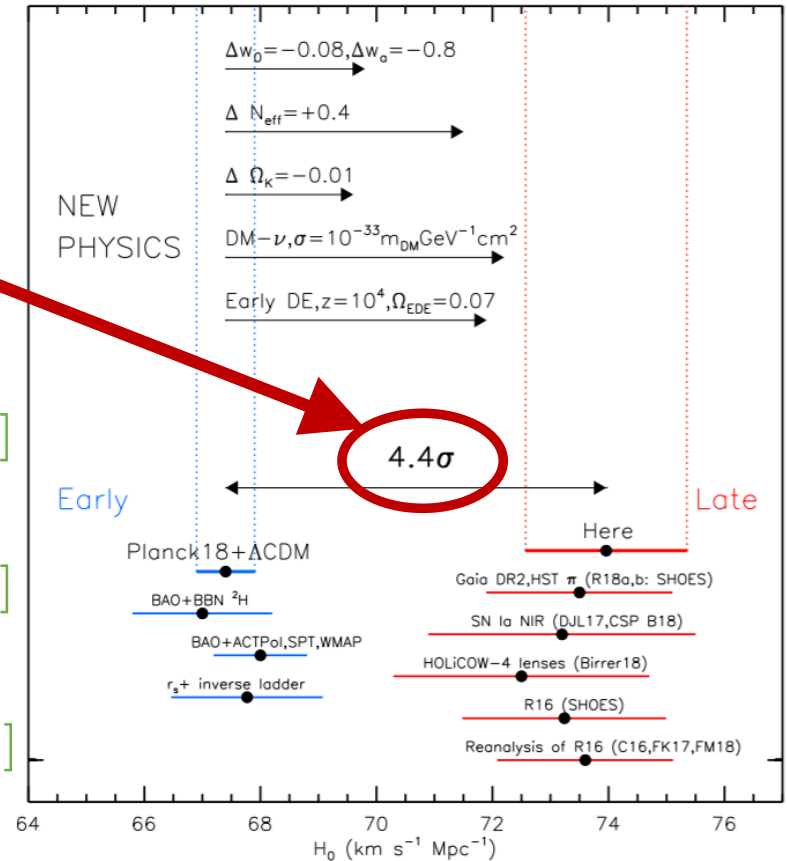
- Tension **unlikely** generated by **CMB** systematics
[Verde *et al.* 1601.01701]
- Local measurement have been **checked against systematics**
[Follin & Knox 1707.01175]
- Discrepancy **also present** with **BAO**
[Addison 1707.06547]

The Hubble tension

- Latest determination of H_0 based on HST : $H_0 = 74.03 \pm 1.42 \text{ km s}^{-1} \text{ Mpc}^{-1}$

- Possible solutions ?

- Early dark energy
[Poulin et al. 1811.04083]
- Decaying dark matter
[Bringmann et al. 1803.03644]
- Goldstones as dark radiation
[Weinberg 1305.1971]
- Non-zero curvature

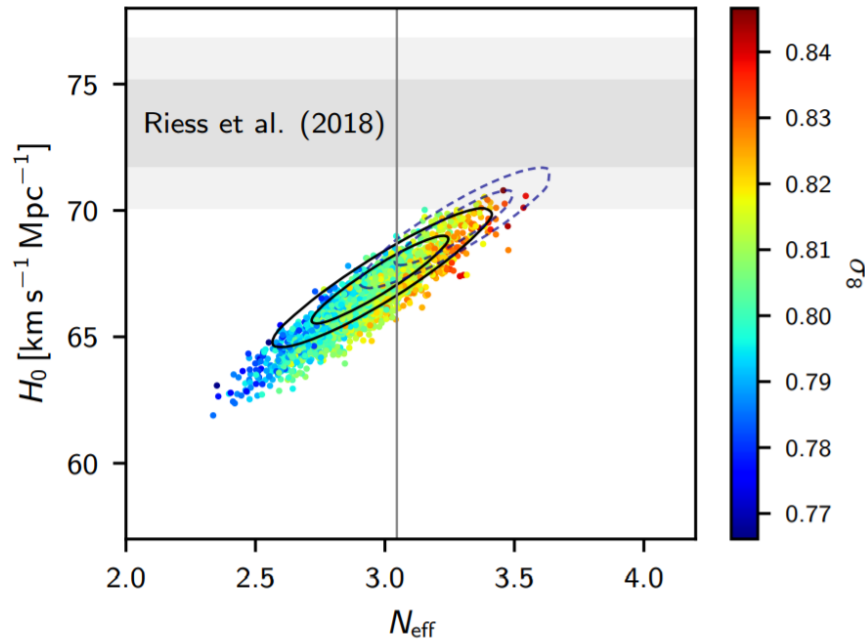


[Riess et al. 1903.07603]

- future Gaia data will **increase** precision on **local** determination of H_0
- Stage-IV CMB experiment expected to deliver $\sigma N_{\text{eff}} \sim 0.03$

The Hubble tension : $\Delta N_{\text{eff}} > 0$?

- Modifying N_{eff} before recombination changes the **sound horizon**, that can be **compensated** by a **larger H_0** for keeping the same **acoustic angular scale**



- Planck+BAO+RIESS18

$$N_{\text{eff}} = 3.27 \pm 0.15$$

$$H_0 = (69.32 \pm 0.97) \text{ km s}^{-1} \text{Mpc}^{-1}$$

[Planck 1807.06209]

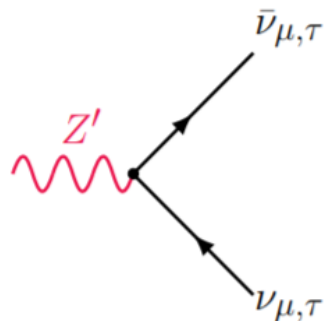
- $\Delta N_{\text{eff}} < 0.53$ from Planck \rightarrow sterile ν interpretation ?
- $2.3 < N_{\text{eff}} < 3.5$ from BBN [Cyburt et al. 1505.01076]

$\Delta N_{\text{eff}} = 0.2 - 0.5$ alleviates the H_0 tension

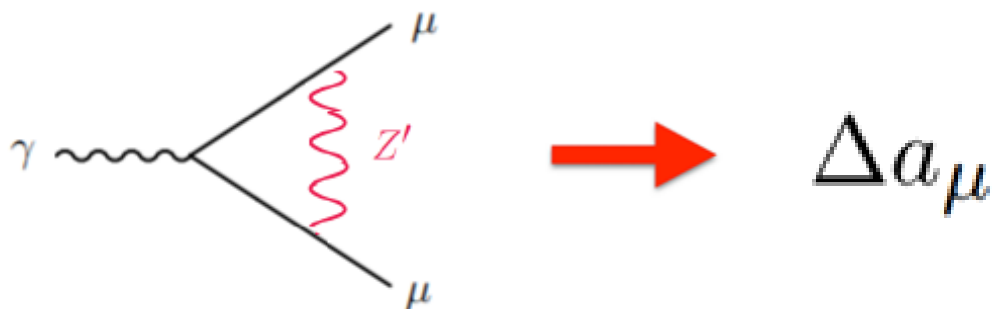
The main idea

Consider the generation of $\Delta N_{\text{eff}} > 0$ from interactions and decay of a light neutrophilic Z' gauge field

$$N_{\text{eff}} \equiv \frac{8}{7} \left(\frac{11}{4} \right)^{4/3} \left(\frac{\rho_{\text{rad}} - \rho_{\gamma}}{\rho_{\gamma}} \right)$$



$$\longrightarrow T_{\nu} > T_{\nu}^{\text{SM}} \longrightarrow \Delta N_{\text{eff}} > 0$$



$$\longrightarrow \Delta a_{\mu}$$

$$\Delta N_{\text{eff}} > 0, N_{\nu} = 3, N_{\text{DR}} = 0, \Delta a_{\mu}$$

A light $L_\mu - L_\tau$ gauge boson

- Assuming a **local** U(1) gauged $L_\mu - L_\tau$ number

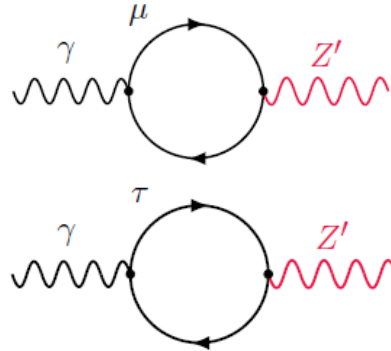
$$\mathcal{L}_{\text{int}} = g_{\mu-\tau} Z'_\alpha (\bar{\mu} \gamma^\alpha \mu + \bar{\nu}_\mu \gamma^\alpha P_L \nu_\mu - \bar{\tau} \gamma^\alpha \tau - \bar{\nu}_\tau \gamma^\alpha P_L \nu_\tau)$$

- Simple **anomaly-free** BSM extension : **2 parameters**

$$10^{-15} < g_{\mu-\tau} < 10^{-1}$$

$$1 \text{ eV} < m_{Z'} < 2m_\mu$$

- Kinetic mixing**

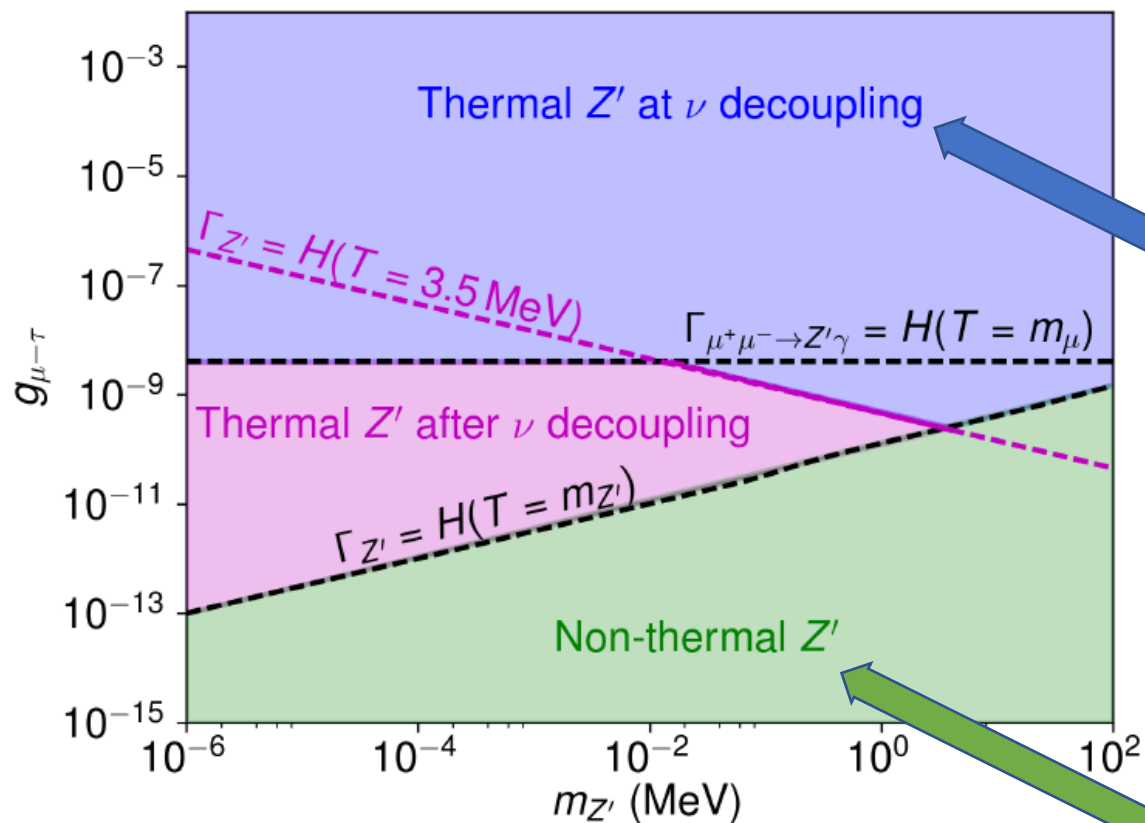


$$\epsilon = -\frac{eg_{\mu-\tau}}{12\pi^2} \log \frac{m_\tau^2}{m_\mu^2} = -\frac{g_{\mu-\tau}}{70}$$

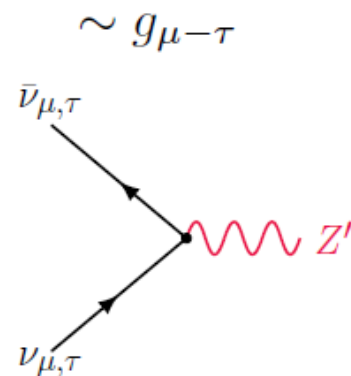
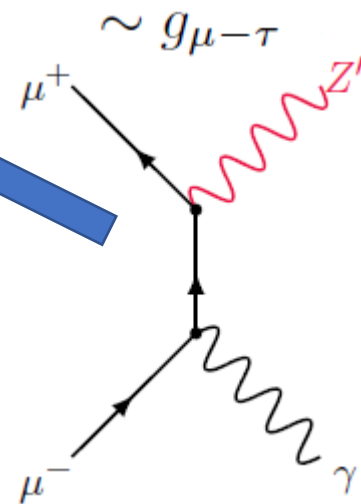
- Neutrinophilic** $\Gamma_{Z' \rightarrow \bar{\nu}_i \nu_i} = \frac{g_{\mu-\tau}^2 m_{Z'}^2}{24\pi}$

- Coupling to electrons** $\text{Br}_{Z' \rightarrow e^+ e^-} \simeq 2 \times 10^{-5}$

A light $L_\mu - L_\tau$ gauge boson



Key processes



3 regimes :

- Thermal Z' at ν decoupling
- Thermal Z' after ν decoupling
- Non-thermal Z'

The thermal regime

- Z' in thermal equilibrium with ν due to large coupling

$$T_{Z'} = T_\nu$$

- ν -oscillations are active at $T \sim 3$ MeV :

$$T_\nu \equiv T_{\nu_\mu} = T_{\nu_\tau} = T_{\nu_e}$$

- Need to solve

[Escudero 1812.05605]

$$\frac{dT_\nu}{dt} = - \left(4H\rho_\nu + 3H(\rho_{Z'} + p_{Z'}) - \frac{\delta\rho_\nu}{\delta t} - \frac{\delta\rho_{Z'}}{\delta t} \right) \left(\frac{\partial\rho_\nu}{\partial T_\nu} + \frac{\partial\rho_{Z'}}{\partial T_\nu} \right)^{-1}$$

$$\frac{dT_\gamma}{dt} = - \left(4H\rho_\gamma + 3H(\rho_e + p_e) + \frac{\delta\rho_\nu}{\delta t} + \frac{\delta\rho_{Z'}}{\delta t} \right) \left(\frac{\partial\rho_\gamma}{\partial T_\gamma} + \frac{\partial\rho_e}{\partial T_\gamma} \right)^{-1},$$

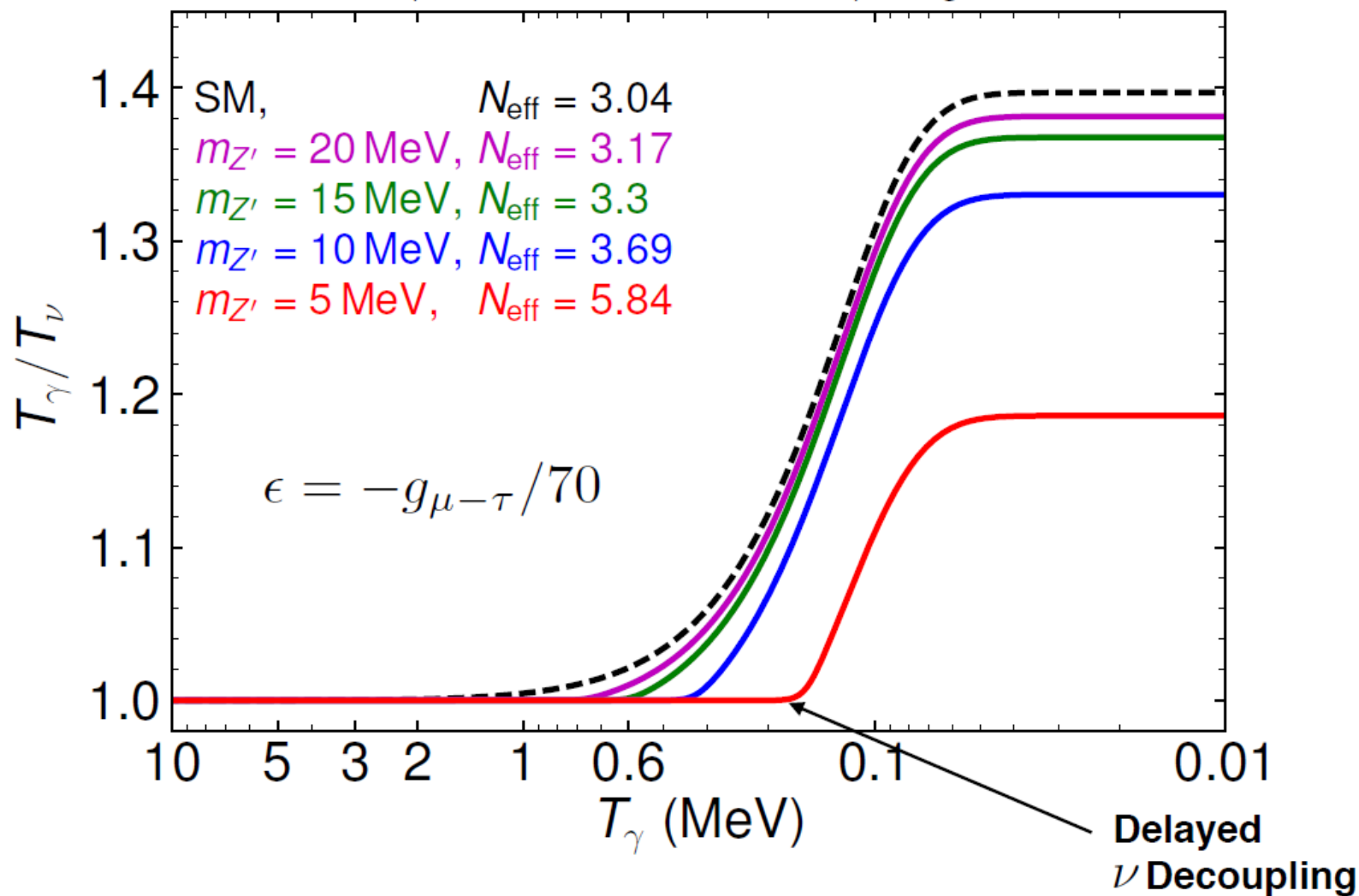
- Need to compute thermal averaged rates

$$e^+ e^- \leftrightarrow \bar{\nu} \nu$$

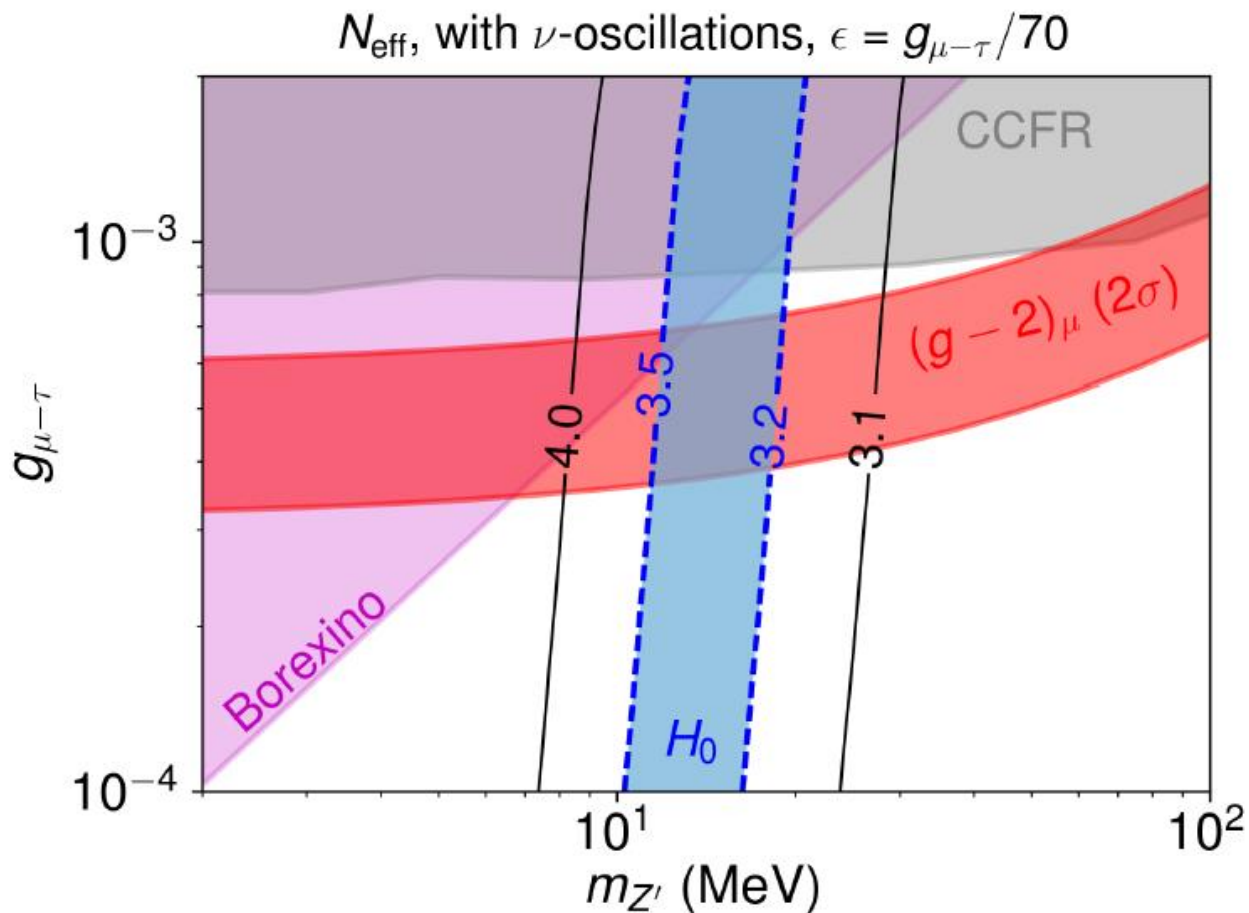
$$Z' \leftrightarrow e^+ e^-$$

The thermal regime

$$g_{\mu-\tau} = 4 \times 10^{-4} \simeq g_{\mu-\tau} |_{g-2}$$



The thermal regime

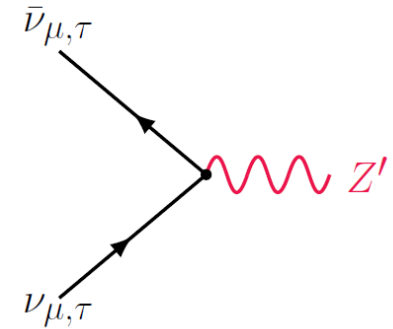


- **Compatible** with simultaneous H_0 and $(g - 2)_{\mu}$!

$$m_{Z'} \simeq 10 - 20 \text{ MeV} \quad g_{\mu-\tau} \simeq (4 - 8) \times 10^{-4}$$

Weakly coupled regime

- For **small couplings**, no early thermal Z' -SM equilibrium, only **one** relevant process
- **Non-thermal !** Need the full phase space distribution



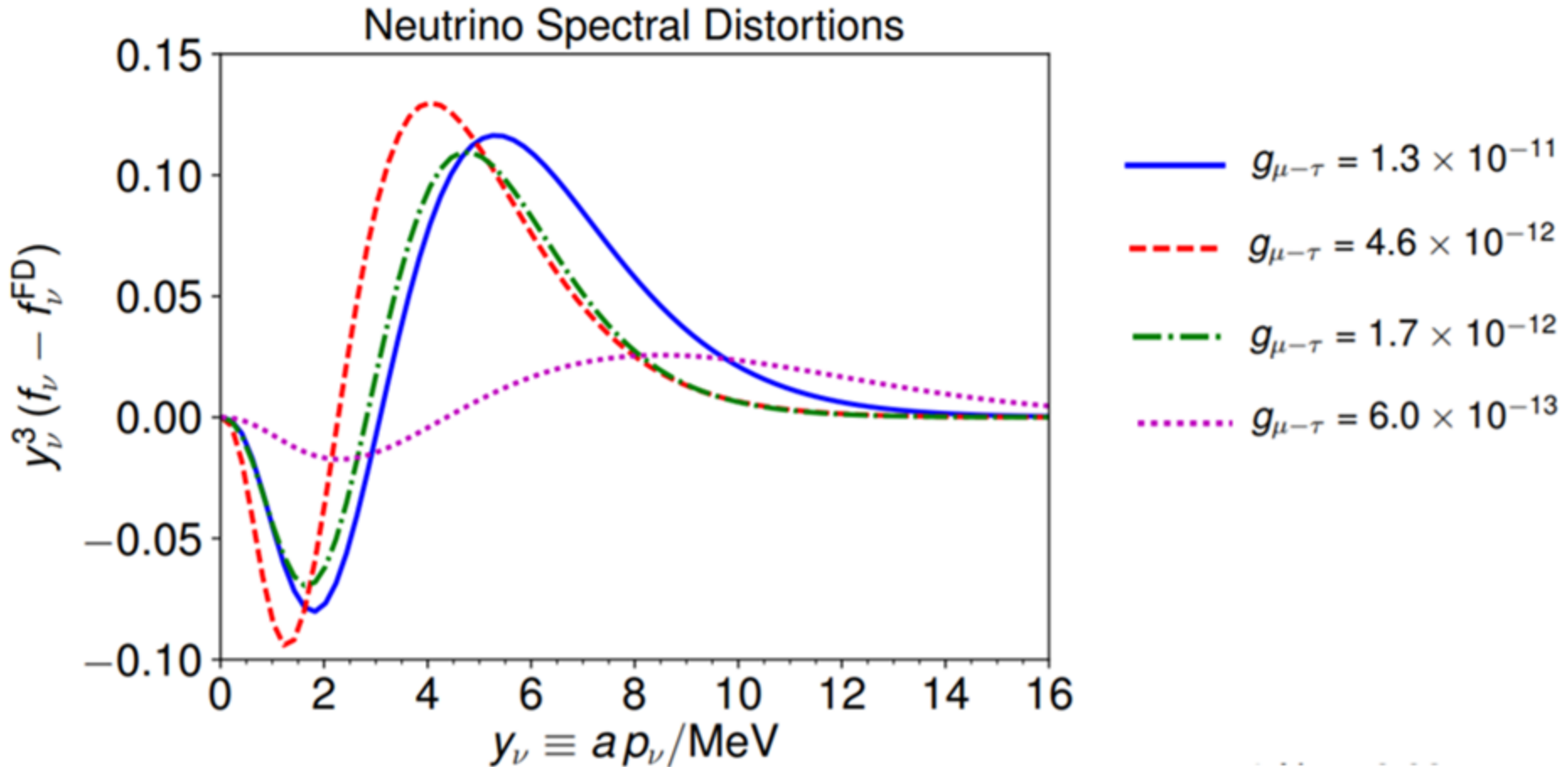
$$\frac{\partial f_{Z'}}{\partial t} - H p_{Z'} \frac{\partial f_{Z'}}{\partial p_{Z'}} = -\frac{m_{Z'} \Gamma_{Z'}}{E_{Z'} p_{Z'}} \int_{\frac{E_{Z'} - p_{Z'}}{2}}^{\frac{E_{Z'} + p_{Z'}}{2}} dE_{\nu} F_{\text{dec}}(E_{Z'}, E_{\nu}, E_{Z'} - E_{\nu}),$$

$$\frac{\partial f_{\nu}}{\partial t} - H p_{\nu} \frac{\partial f_{\nu}}{\partial p_{\nu}} = \frac{m_{Z'} \Gamma_{Z'}}{E_{\nu} p_{\nu}} \int_{|(m_{Z'}^2/4p_{\nu}) - p_{\nu}|}^{\infty} \frac{dp_{Z'} p_{Z'}}{E_{Z'}} F_{\text{dec}}(E_{Z'}, E_{\nu}, E_{Z'} - E_{\nu})$$

with $F_{\text{dec}}(E_{Z'}, E_{\nu_1}, E_{\nu_2}) = f_{Z'}(E_{Z'}) [1 - f_{\nu}(E_{\nu_1})] [1 - f_{\nu}(E_{\nu_2})] - f_{\nu}(E_{\nu_1}) f_{\nu}(E_{\nu_2}) [1 + f_{Z'}(E_{Z'})]$.

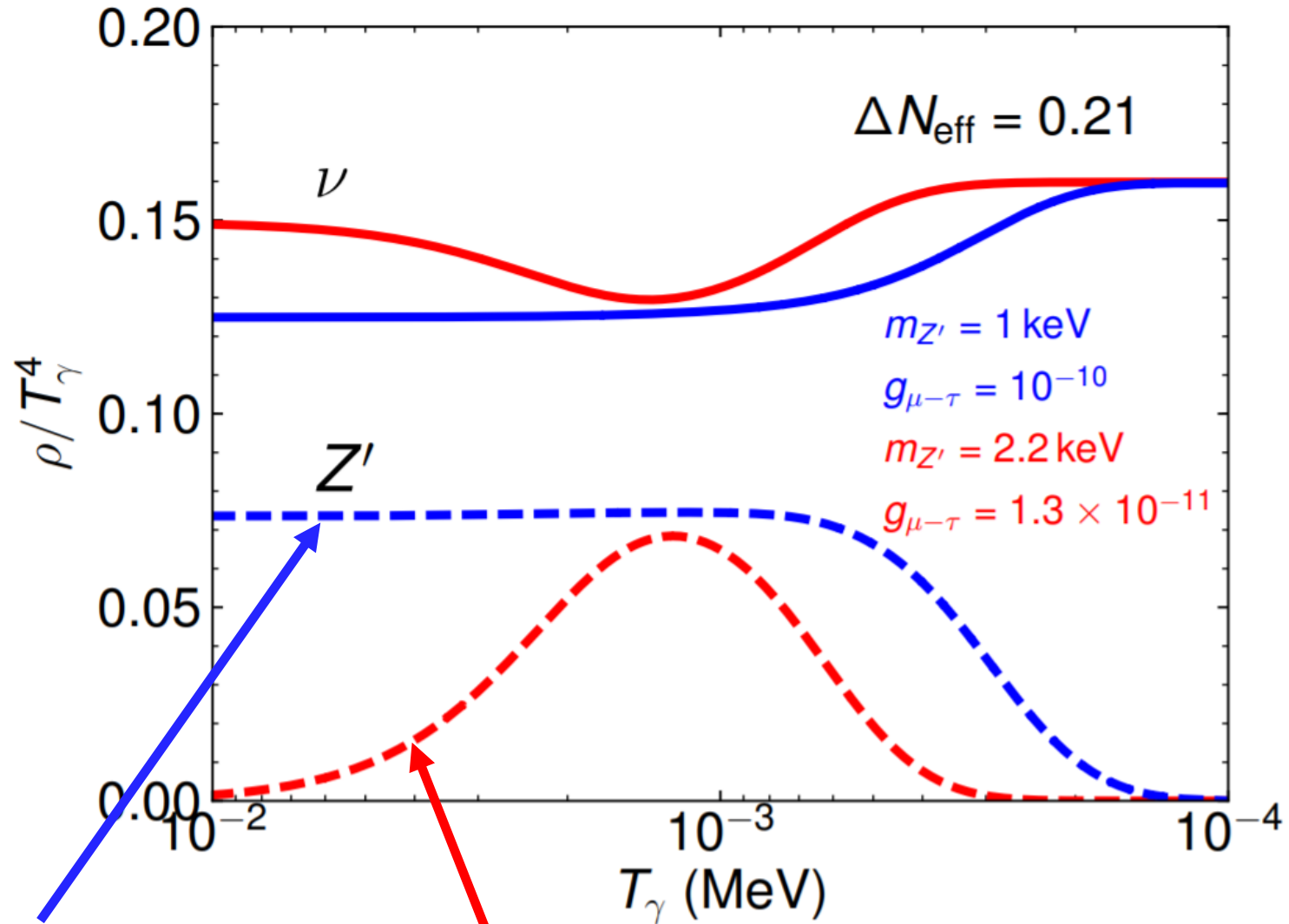
- **Stiff** set of equations, solved for **100 bins** in comoving momentum for the Z' and ν distributions
- Check **continuity equation** $\frac{d\rho}{dt} = -3H(\rho + p)$

The ν phase space distribution



- **Non-thermal** distribution : our approach is justified !

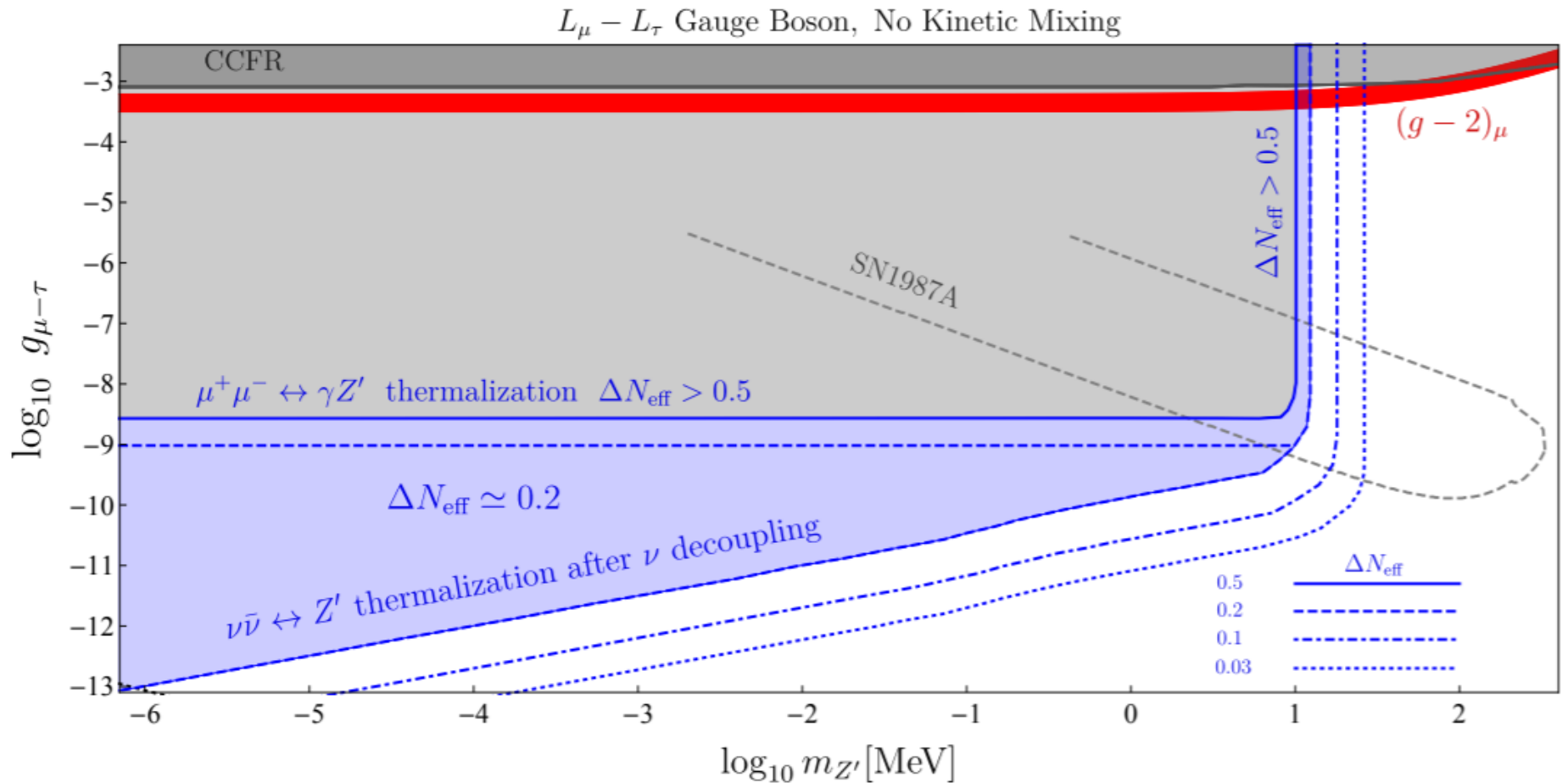
Weakly coupled regime



thermalized

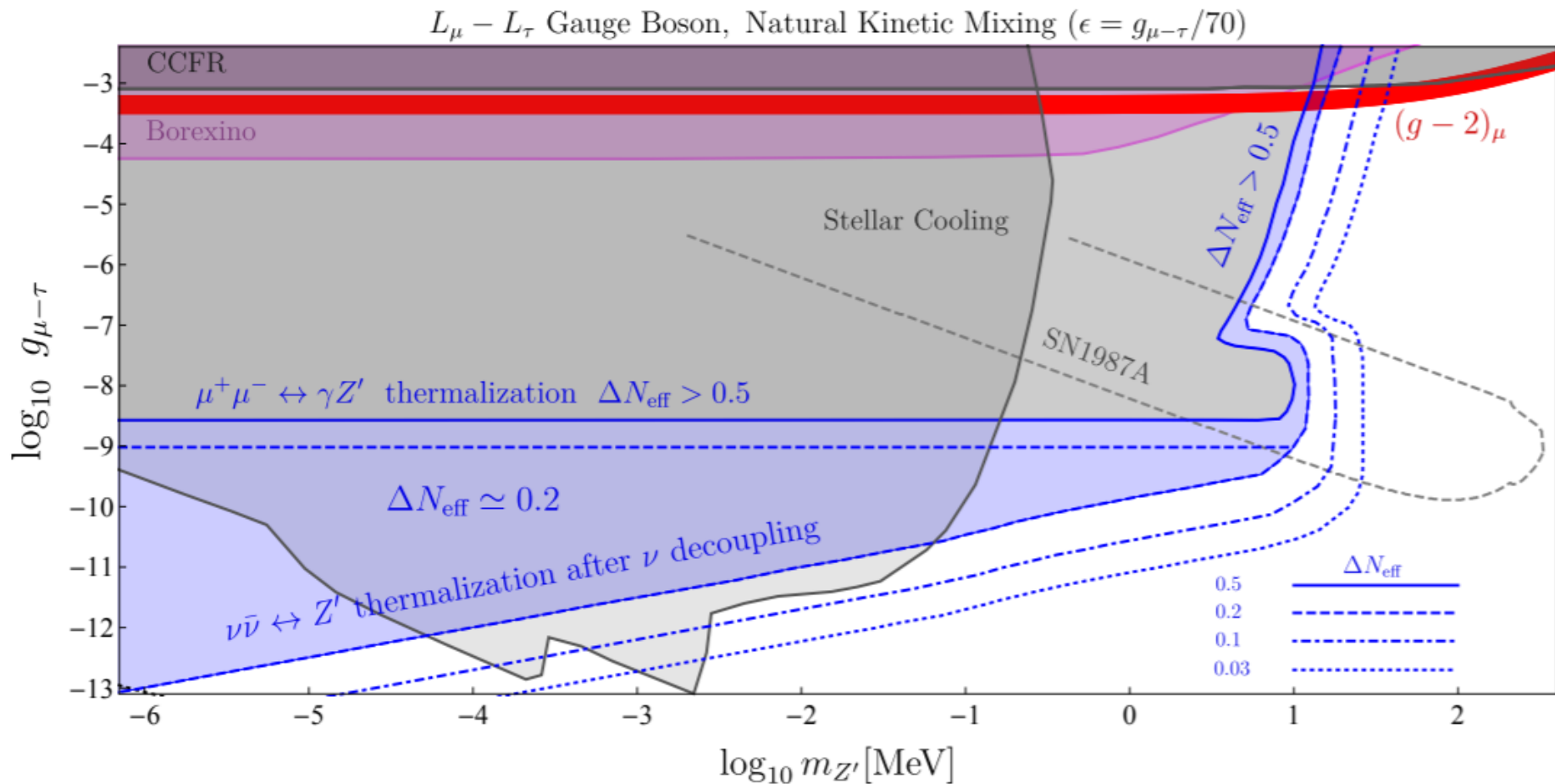
non-thermalized

The results



- $\Delta N_{\text{eff}} = 0.21$ over a **large plateau** of parameter space
- Due to **secluded ν - Z' system** after ν -decoupling and **out-of-equilibrium decay**

The results



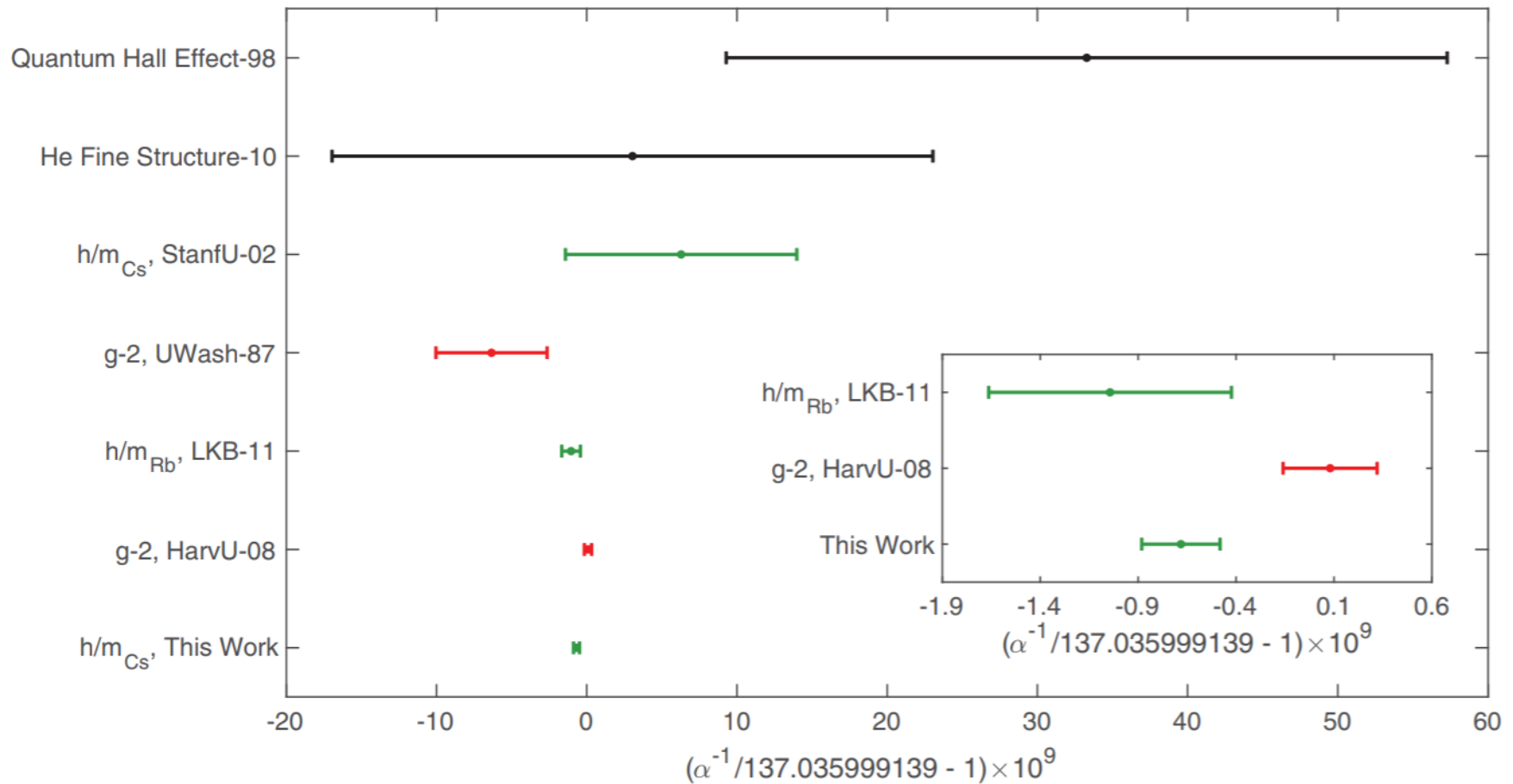
- **Stellar cooling** important when **kinetic mixing** considered
- For $m_{Z'} < 100$ keV : $\Delta N_{\text{eff}} = 0.21$ at CMB but $\Delta N_{\text{eff}} = 0$ at BBN !

Take-home message

- The H_0 and $(g - 2)_\mu$ **tensions** : physics **beyond** Λ CDM?
- H_0 and $(g - 2)_\mu$ **tensions** can be simultaneously addressed for
$$m_{Z'} \simeq 10 - 20 \text{ MeV} \quad g_{\mu-\tau} \simeq (4 - 8) \times 10^{-4}$$
- $\Delta N_{\text{eff}} = 0.21$ a generic prediction of a light L_μ - L_τ gauge boson
- **Local measurements** of H_0 expected to deliver a precision of $\sim 1\%$ within the **next few years**
- The $\Delta N_{\text{eff}} \sim 0.2 - 0.5$ hypothesis could be **tested** at **stage-IV** CMB experiments, expected to deliver $\sigma N_{\text{eff}} \sim 0.03$
- Very reach interplay between particle physics and cosmology

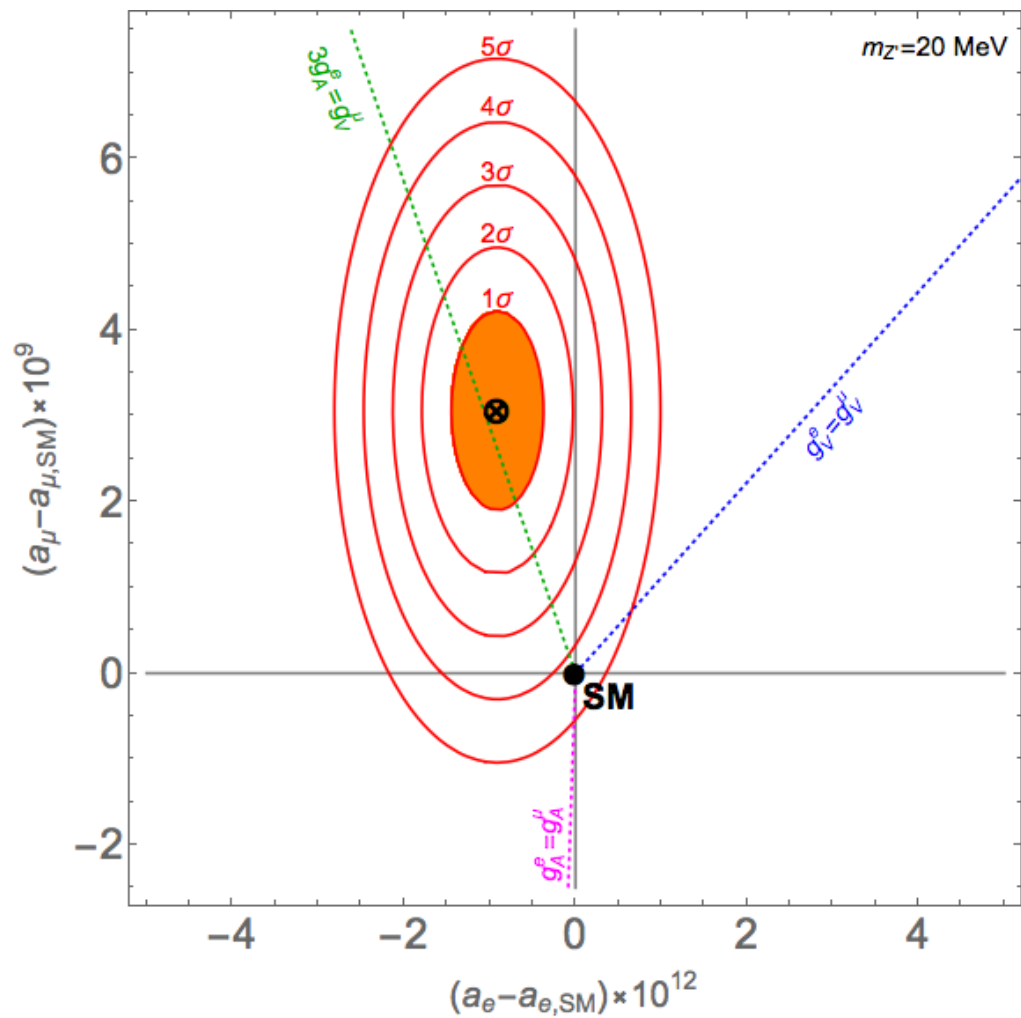
Back-up Slides

The $(g - 2)_e$ anomaly



[Parker, R. H., Yu, C., Zhong, W., Estey, B., & Müller, H. (2018). *Measurement of the fine-structure constant as a test of the Standard Model*. *Science*, 360(6385), 191–195.]

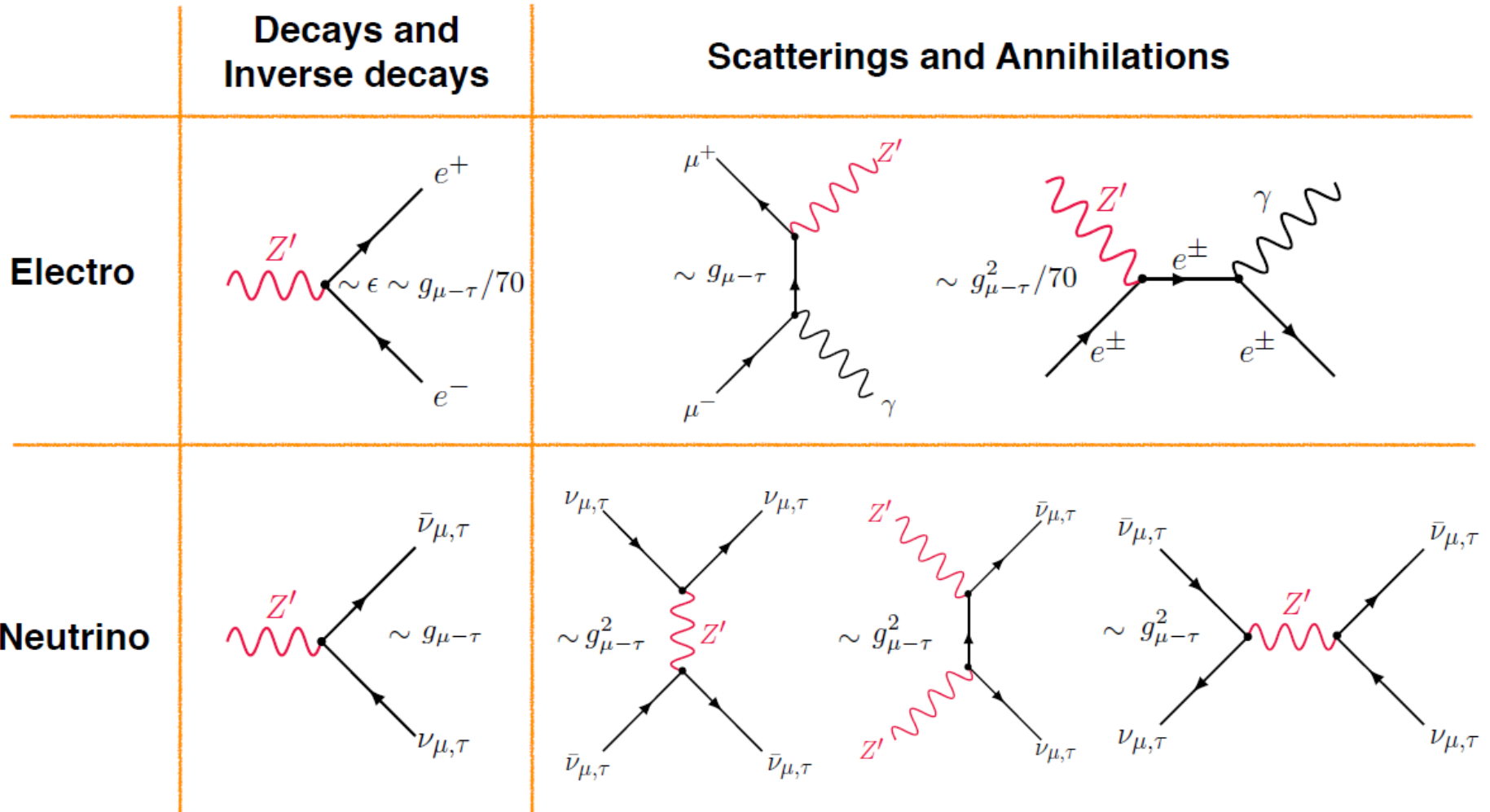
The $(g - 2)_e$ anomaly



[Adam Falkowski's blog *Resonaances*]

A light $L_\mu - L_\tau$ gauge boson

- Z' in kinetic equilibrium with e^\pm, γ, ν ?



ν – decoupling and N_{eff}

- ν -decoupling T_d when $n_\nu \langle \sigma v \rangle \sim H$

with $n_\nu \langle \sigma v \rangle \simeq G_F^2 T^5$

$$T_d \sim 1 \text{ MeV}$$

- $N_{\text{eff}} \equiv \frac{8}{7} \left(\frac{11}{4} \right)^{4/3} \left(\frac{\rho_{\text{rad}} - \rho_\gamma}{\rho_\gamma} \right)$

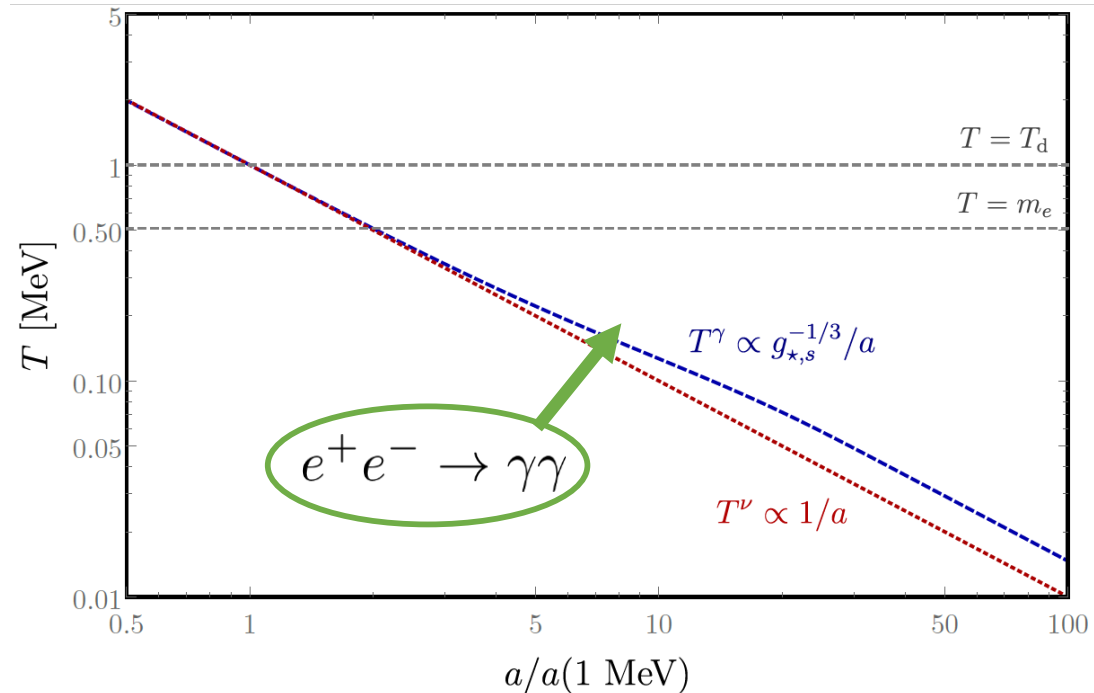
- $N_{\text{eff}} = 3 \left(\frac{11}{4} \right)^{4/3} \left(\frac{T_\nu}{T_\gamma} \right)^4$

- $N_{\text{eff}}^{\text{SM}} = 3.045$ [Salas & Pastor 1606.06986]

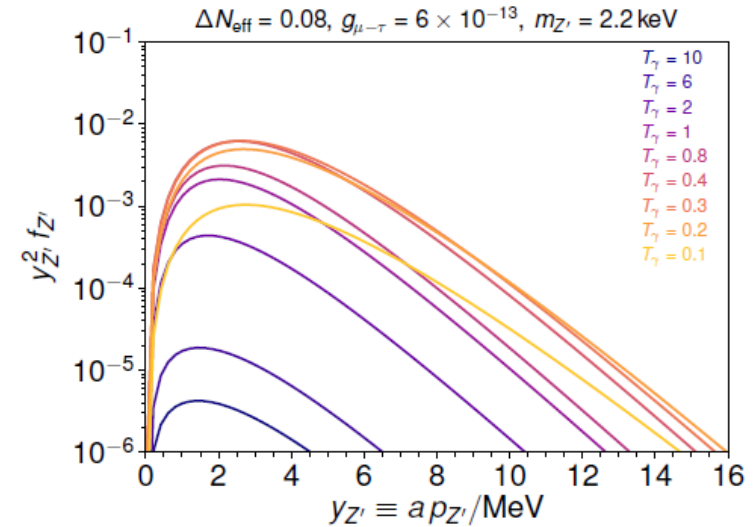
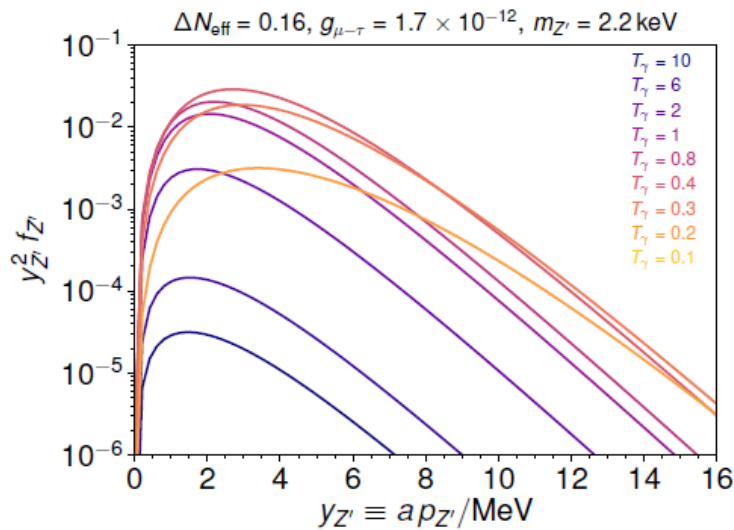
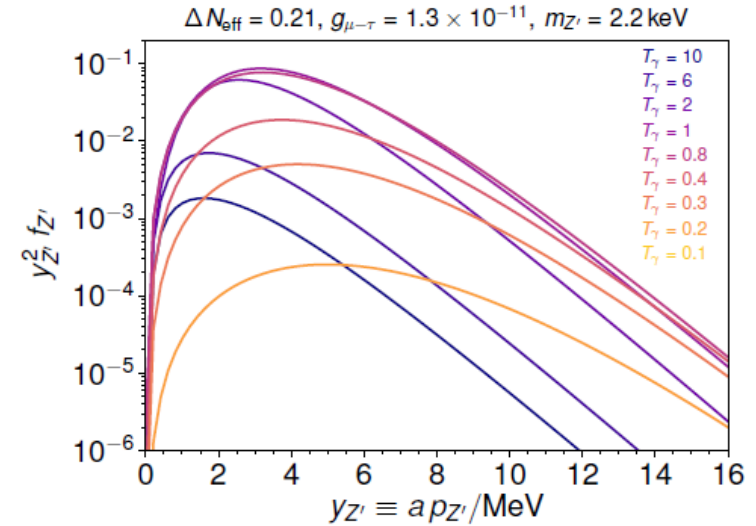
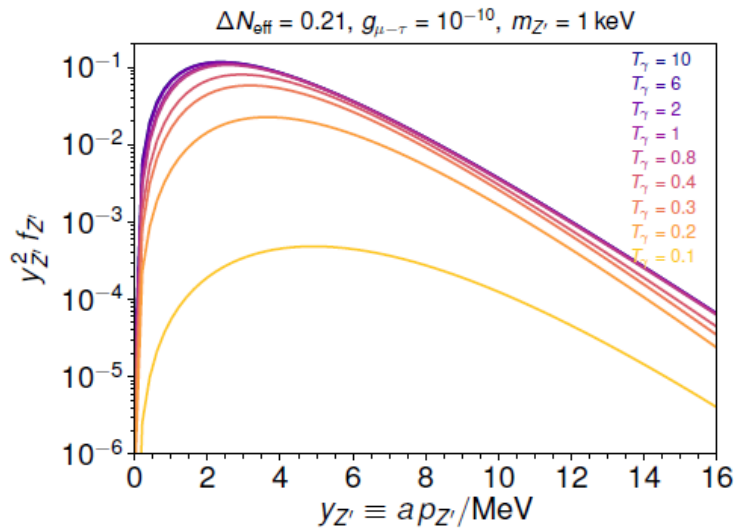
- Why $N_{\text{eff}} \neq 3$?

[Dolgov 0202122]

- $T_d \neq 1 \text{ MeV}$
- Non-instantaneous decoupling
- ν -oscillations
- QED finite temperature corrections



Phase space distribution



Constraints

Laboratory constraints

Neutrino Tridents	Relevant for large couplings and large masses
Kaon decays	Relevant if no kinetic mixing
B-factories	Relevant for the g-2 anomaly region
Beam dumps	Absent due to $\text{Br}_{Z' \rightarrow e^+e^-} \simeq 2 \times 10^{-5}$
Solar neutrino scatterings	Relevant for the g-2 anomaly region

Astrophysical constraints

SN1987A	Very important in a considerable portion of parameter space
Stellar Cooling	Very important in a considerable portion of parameter space

Cosmological constraints

Energy injection at the CMB	Absent due to $\text{Br}_{Z' \rightarrow e^+e^-} \simeq 2 \times 10^{-5}$
Energy injection during BBN	Absent due to $\text{Br}_{Z' \rightarrow e^+e^-} \simeq 2 \times 10^{-5}$

The $(g - 2)_\mu$ anomaly

History of $(g - 2)_e$

$$\vec{\mu}_e = g_e \frac{\sqrt{4\pi\alpha}}{2m_e} \vec{S}_e$$

- **1948 Schwinger** $(g - 2)_e/2 \simeq \alpha/(2\pi)$

$$(g - 2)_e^{\text{exp}}/2 = 1\,159\,652\,180.73(28) \times 10^{-12}$$

[Hanneke et al. 0801.1134]

- **2008**

$$(g - 2)_e^{\text{SM}}/2 = 1\,159\,652\,181.61(23) \times 10^{-12}$$

[Aoyama et al. 1712.06060]

- **2018 : $\sim 2\sigma$ discrepancy in $(g - 2)_e$?**

[Parker et al. 1812.04130]

Contents

- I. Motivation : H_0 and $(g - 2)_\mu$**
 1. The $(g - 2)_\mu$ discrepancy
 2. The H_0 tension
 3. ν -decoupling and N_{eff}

- II. A very light L_μ - L_τ gauge boson**
 1. The model
 2. Main processes and regimes

- III. Results and conclusion**